Compaction of Plasmid DNA by Macromolecular Crowding

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Supporting Information

ABSTRACT: With a view to understand compaction of DNA in crowded conditions, we have measured the radius of gyration of pHSG298 plasmid (2675 bp) in its supercoiled and linear forms and in the presence of dextran nanoparticles with light scattering. It was observed that the supercoil initially expands and subsequently compacts with increasing volume fraction of the crowder. The extent of the expansion depends on the size of the nanoparticle, with the smallest particles exhibiting the largest effect. In the case of the linear plasmid, monotonous compaction and no apex in the radius of gyration were observed. The plasmid does not collapse into a condensed state. In crowded conditions, the size of the supercoiled molecule exceeds the one of its linear variant. Supercoiling hence restrains rather than facilitates compaction of crowded DNA. Our results show two different, but closely related, aspects of the crowding phenomenon. First, the supercoil expands through a modification of its geometrical properties by the depletion induced attraction between the two opposing duplexes of the superhelix. Second, the molecule gets compressed due to the depletion of nanoparticles in the interior of the coil with concomitant imbalance in osmotic pressure between the coil and surrounding medium. The antagonistic nature of these two aspects of crowding results in a much more pronounced and richer effect on the dimensions of supercoiled plasmid than the effect of variation in ionic strength. The change in DNA dimensions as a response to crowding may have implications in biology as well as biotechnology.

INTRODUCTION

DNA often exists in a supercoiled conformation, in which the duplex is wound around itself to form a higher order helix.1 It is also often congested, such as in liquid crystals, the nucleolus of bacterial cells, synthetic gene transfer vectors, and porous gel materials for size exclusion chromatography.2−6 The conformation of the supercoil is determined by topological and geometrical properties (degree of interwinding and number of interwound branches), concentration of salts, interaction among DNA molecules at higher concentrations, and interaction with other biomolecules including neutral crowders. In order to be accommodated in a crowded state, the supercoil has to decrease its spatial extent (excluded volume) by a change in conformation. Correspondingly, DNA’s conformation is modulated in response to changes in crowding through the effect on excluded volume. This plasticity of DNA shapes may have a regulatory role and be important for the postreplicative segregation of bacterial chromosomes.7

Supercoiled DNA can be visualized by (cryo)electron and atomic force microscopy.8,9 It has been observed that the distance between the two opposing duplexes in the superhelix (interduplex distance) is inversely proportional to the superhelical density and decreases with increased concentration of salt. These imaging techniques are however not well adapted to the investigation of three-dimensional solution properties such as excluded volume. Size-related properties are best and quantitatively inferred from scattering experiments using liquid samples representative of the native state. The interwound conformation of supercoiled plasmid (2.7 kbp) has previously been investigated with small-angle neutron scattering.10−12 It was found that the interduplex distance decreases with increased salt and/or DNA concentration (DNA−DNA crowding). The overall size of the supercoil, that is, its radius of gyration \( R_g \), can be determined by static light scattering. With this method it was found that supercoiled plasmid has a 30−45% smaller size than its linear isoform, but no significant change in \( R_g \) with concentration of salt was observed.13−15 Note that these results were obtained for DNAs dispersed in solutions of salts without crowding agents.

Here, we investigate the compaction of a supercoiled plasmid (pHSG298, 2675 bp) by the generic crowding agent dextran. In the present buffer conditions, the molecules do not collapse into a condensed state. Dextran is a neutral branched polysaccharide made of glucose monomers. The dextran molecules used in this study have a radius of gyration \( d \) in the range 2.6−17 nm. They are spherical nanoparticles and readily dissolve in water. Dextran is often used to mimic the intracellular crowded environment in vitro.16 We isolated and purified plasmid in the supercoiled and linear isoforms. These isoforms were dispersed in an aqueous buffer with various amounts of dextran, and their sizes (\( R_g \)) were measured with Rayleigh light scattering. Sufficiently diluted samples were used...
to ensure minimal inter-DNA interference and minimal effect of DNA–DNA crowding on the conformation of the plasmids. For reference, \( R_g \) of the plasmids in crowd-free solution, but in the presence of various concentrations of salt, was also measured. The results are discussed in terms of the geometric properties of the supercoil as well as osmotic effects induced by the depletion interaction between DNA and the crowding nanoparticles.

### EXPERIMENTAL PROCEDURES

#### Preparation of the Cell Paste

BL21 bacteria transformed with pHSG298 were grown on a Luria Broth (LB) plate with kanamycin (25 mg/L). A single colony was taken to grow a starter culture in LB medium containing kanamycin at 310 K for 8 h (\( \text{OD}_{600} = 0.8 \)). The starter culture was diluted 1000 times into LB medium containing kanamycin and grown at 310 K for 12 h to get to the desired cell density (\( \text{OD}_{600} = 1.8 \) for each batch). The cells were harvested by centrifugation at 6000×g for 15 min at 277 K.

#### Plasmid Extraction and Purification

The bacterial pellet was suspended in 0.5 L of 50 mM Tris-Cl buffer, pH 7.5, 10 mM EDTA, and subsequently lysed with 0.5 L of an alkaline solution (0.2 M NaOH, 1% SDS) at room temperature. The pH of the Cell suspension and the alkaline solution was maintained below 12.5. Genomic DNA, cell debris, and proteins were precipitated by adding 0.5 L of 3 M potassium acetate, pH 5.5, prechilled at 277 K. After centrifugation at 20000×g for 30 min at 277 K, the supernatant was pumped through a Sepharose 6 fast flow column (XX 50/30) equilibrated with 2 M (NH₄)₂SO₄, 10 mM EDTA, and 100 mM Tris-Cl, pH 7.0, with an AKTA explorer chromatography system (GE Life Sciences, columns and chromatography media were also purchased from GE). This gel filtration step results in the removal of RNA. The plasmid was further purified by thiophilic interaction chromatography using a column with PlasmidSelect, equilibrated with the above-mentioned 2 M (NH₄)₂SO₄ buffer, and eluted with a gradient to 0.4 M NaCl, 2 M (NH₄)₂SO₄ 10 mM EDTA, and 100 mM Tris-Cl, pH 7.0. Finally, the sample was concentrated and endotoxins were removed by capturing the plasmid on a Source 30Q ion exchange column followed by elution in a gradient to 0.6 M NaCl. After precipitation with isopropanol, the DNA was gently dried for a short period, dissolved in 1×TE (10 mM Tris, 1 mM EDTA, pH 8) buffer, and stored at 277 K. We have obtained a reasonably good quality of the supercoiled plasmid by optimization of the purification protocol through a longer concentration gradient in the elution of the Sepharose column. As byproduct, we obtained the purified pHSG298 plasmid in the linearized form.

#### Plasmid Characterization

UV spectroscopy showed that the ratio of the optical absorbance at 260 and 280 nm (\( A_{260}/A_{280} \)) exceeded 1.8, indicating that the preparation was free of protein. The integrity of the plasmid was checked with 0.8% agarose electrophoresis gel in TAE buffer (40 mM Tris-acetate, 1 mM EDTA, pH 8.3) at 70 V for 2 h. The gel image is shown in Figure S1. The linking number deficit and percentage of open circular plasmid were determined by a series of 1.4% agarose electrophoresis gels in TPE buffer (90 mM Tris-phosphate, 1 mM EDTA, pH 8.3) at 50 V for 36 h with chloroquine phosphate concentrations of 1, 3, 5, 10, 20, 40, 80, and 120 mg/L. The positions of the bands pertaining to \( \Delta L_k = 0 \) and \( \pm 1 \) were determined by (partial) relaxation of the plasmid with topoisomerase II (Affymetrix). We observed optimal separation of the topoisomer at chloroquine phosphate concentrations of 3 and 80 mg/L. At these concentrations all topoisomers are either negatively (3 mg/L) or positively (80 mg/L) supercoiled. The gel images obtained with chloroquine phosphate concentrations of 1, 3, and 80 mg/L are shown in Figure S2. In the series of gels with increasing concentration of the intercalator, we counted a linking number deficit \( \Delta L_k = -9 \pm 2 \) (superhelical density \( \sigma = -0.035 \)) pertaining to the most abundant topoisomer. About 5% of the plasmid is nicked and open circular.

#### Sample Preparation

All samples were prepared with a final DNA concentrations \( C_{\text{DNA}} \) of 50 mg/L. Dextran with molecular weights of 50, 500, 50, and 410 kg/mol was purchased from Sigma-Aldrich. The buffer solvents are 0.4×TE with added NaCl and 1×TE with added dextran.

Solutions of supercoiled and linearized plasmid and the relevant solvent were mixed and incubated for at least 24 h at 277 K. Prior to light scattering measurements, solvent and samples were filtered through 0.02 and 0.22 μm Whatman syringe filters, respectively. The final DNA concentration (after filtration) was determined by UV–vis spectroscopy.

#### Light Scattering

Light scattering measurements were done with a Wyatt DAWN 8+ multiangle light scattering instrument (Goleta, CA). The incident light source was a GaAs diode laser (50 mW) generating vertically polarized light of 658 nm wavelength. Scattered light is simultaneously measured by eight photodetectors at angles spaced between 15° and 160° with respect to the incident beam. This allows a momentum transfer range of \((0.3−2.5) \times 10^{-7} \text{nm}^{-1}\). The plasmid samples were slowly injected into the flow cell of the light scattering instrument to avoid any structural changes due to pressure. A baseline was determined by measuring the scattering from the buffer at the beginning as well as at the end of the sample injection. Data reduction with Wyatt’s ASTRA software allowed subtraction of the baseline solvent scattering and the determination of the excess Rayleigh ratio \( R_0 \).

### RESULTS

For pHSG298 plasmid, with dimensions of less than 100 nm, the overlap concentration between the dilute and the semidilute regime is around 3 g/L. The latter concentration exceeds the concentration employed in the light scattering experiments (50 mg of DNA/L) by 2 orders of magnitude. At such a low concentration interference among different DNA molecules is negligible (to be confirmed below). Furthermore, we have checked that the scattered intensity recorded at an angle of 90° from a plasmid solution and a typical mixture of plasmid and dextran exceeds the intensity pertaining to the corresponding dextran solution by a factor of 30 and 40, respectively. Accordingly, the scattering is dominated by DNA and the contribution from dextran is negligible. The excess Rayleigh ratio is then proportional to the DNA form factor \( P(q) \) according to \( R_0 = K^* cM P(q) \), with \( K^* \) an optical constant, \( c \) the concentration of DNA, and \( M \) the DNA molar mass.

### Figure 1

(A) Partial Zimm plot for linear plasmid in 1×TE with 2 g/dextran/L. Dextran size \( d = 2.6 \text{ nm} \). (B) As in panel A, but for supercoiled plasmid in 1×TE with 2 g/dextran/L and dextran size \( d = 6.9 \text{ nm} \). The curves represent fits of the relevant form factors.
supercoiled plasmid in 1×TE (10 mM Tris, 1 mM EDTA, pH 8) buffer, respectively. Note that $P(q)$ is normalized to unity for $q \to 0$, so that $M_w$ can be obtained from the y-axis intercept. The radius of gyration $R_g$ is obtained from a fit of the relevant form factor $P(q)$ to $K^6c/R_g$ at higher values of momentum transfer.

For the linear isoform, the data are analyzed with an approximate $P(q)$ pertaining to a linear, semiflexible polymer with excluded volume effects. To the best of our knowledge, a general expression for $P(q)$ of supercoiled DNA is not available. Our previously reported expression is only valid for high values of $q$ exceeding the inverse interduplex distance. The present light scattering experiments are performed in the low $q$ range with $0.25 < qR_g < 2$. Furthermore, our closed circular plasmid is moderately supercoiled (superhelical density $\sigma \sim -0.035$) and can to a good approximation be considered a semiflexible ring. Accordingly, we have used the low $qR_g$ approximation of $P(q)$ pertaining to a ring polymer with excluded volume interaction. The utilized expressions for $P(q)$ are summarized in the Supporting Information. Examples of the fits are shown in Figure 1. In particular deviations from linearity at larger $q$ range are well described. For dextran-crowded plasmid, the fitted values of $M_w$ are shown in Figure 2. The values of $R_g$ of supercoiled plasmid crowded by dextran of various size are displayed in Figure 3A. For the sake of comparison, $R_g$ pertaining to linear and supercoiled plasmid dispersed in buffers of various ionic strength but without dextran is shown in Figure 3B. The effect of the topological constraint (supercoiled versus linear) on $R_g$ of dextran-crowded plasmid is displayed in Figure 4. We have verified that inclusion of self-avoidance in the data analysis results in no appreciable differences in $M_w$ and marginal differences in $R_g$ of less than 3%.

![Figure 2](image2.png)

**Figure 2.** Molecular mass $M_w$ of linear (magenta ▲, gold ◀) and supercoiled (red ▲, green ◀, blue ▼) plasmid in 1×TE versus dextran volume fraction $\Phi$ of dextran with size $d = 2.6$ nm (red ▲, magenta ▲), 6.9 (green ◀, gold ◀), and 17 (blue ▼) nm. The dashed line denotes the calculated value for pHSG298, that is, $1.78 \times 10^6$ g/mol.

![Figure 3](image3.png)

**Figure 3.** (A) Radius of gyration $R_g$ of supercoiled plasmid in $1 \times$ TE versus volume fraction $\Phi$ of dextran with size $d = 2.6$ (red ▲), 6.9 (green ◀), and 17 (blue ▼) nm. The solid line represents $\Phi^{-1/4}$ scaling. (B) Radius of gyration $R_g$ of linear (blue ▼) and supercoiled (red ▲) plasmid versus ionic strength $I$.

![Figure 4](image4.png)

**Figure 4.** (A) Radius of gyration $R_g$ of linear (blue ▼) and supercoiled (red ▲) plasmid in 1×TE versus volume fraction $\Phi$ of dextran with size $d = 2.6$ nm. (B) As in panel A, but for dextran with size $d = 6.9$ nm.

Based on the base pair sequence, the calculated $M_w = 1.78 \times 10^6$ g/mol. For the dextran-crowded samples, the averaged experimental value $M_w = (1.8 \pm 0.2) \times 10^6$ g/mol. No systematic variation is observed, irrespective DNA topology, dextran size, and volume fraction (see Figure 2). The agreement between the experimental and calculated molecular weights confirms the negligible contribution to the scattering from dextran, insignificant plasmid aggregation or catenation, and insignificant interference among different DNA molecules.

For supercoiled, dextran-free plasmid in 1×TE buffer (ionic strength of 10.7 mM), $R_g$ takes a value of $67 \pm 1$ nm. This value is in fair agreement with the literature $R_g$ values of 102 ± 2, 82 ± 3, and 56 ± 4 nm for S.8, 3.7, and 2.7 kbp supercoiled DNA, respectively. Furthermore, the smaller size of supercoiled plasmid with respect to its linear isofrom (in crown-free conditions) and the moderate decrease in size with increasing ionic strength agree with previously reported results.

The presence of the dextran nanoparticles impacts the size of both supercoiled and linear DNA. In the limit of vanishing volume fraction of dextran, the measured values of $R_g$ in 1×TE buffer approach the values obtained in 0.4×TE buffer with added NaCl at the relevant ionic strength of 10.7 mM. For supercoiled plasmid and smaller dextran size ($d \leq 6.9$ nm), $R_g$ first increases, exhibits an apex, and subsequently decreases with increasing volume fraction of dextran. For the larger dextran particles of size $d = 17$ nm, $R_g$ decreases monotonically and no apex is observed (see Figure 3A). In the case of the linear plasmid and irrespective dextran size, $R_g$ decreases monotonically with increasing volume fraction of dextran (Figure 4). In the present experimental conditions, the plasmid gets compacted but does not collapse into a condensed state (no condensation). For polymer induced condensation, it is necessary to increase the concentration of monovalent salts to hundreds of millimolar and/or to confine the DNA molecule in a nanospace. Since these conditions are not met in our experimental approach, we do not observe a plateau in $R_g$ at high volume fractions of crowder (up to $\Phi = 0.2$). For both supercoiled and linear plasmid, the compaction is highly dependent on nanoparticle size, with the largest particles being...
the most effective. Under minimal or no crowding conditions, the size of supercoiled plasmid is smaller than the size of its linear variant. Accordingly, supercoiling has been identified as a compaction mode, in the sense that it reduces the spatial extent of the molecule. A new result is that in crowded conditions the situation may be reversed. At higher volume fractions of crowder, supercoiled plasmid takes a more extended conformation (larger $R_g$ values) than the linear one. Hence, to a certain extent, supercoiling restrains compaction of DNA by macromolecular crowding. Finally, it should be noted that irrespective topological constraint, the reduction in plasmid size by crowding far exceeds the one caused by an increase in ionic strength (Figure 3).

**DISCUSSION**

Neutral dextran particles with a size of several nanometers penetrate the DNA coil, but they are not known to bind and/or change the mechanical properties of the duplex. However, each segment of the DNA molecule is surrounded by a cylindrical volume in which the nanoparticles cannot penetrate for steric reasons. The effect of this volume interaction is twofold: (i) the geometrical properties of the supercoil change through an attractive force between almost (anti)parallel DNA segments and (ii) the coil gets compressed through an imbalance in osmotic pressure between the interior of the coil and the surrounding medium. The former effect is of particular importance for a superhelix, in which a duplex is wound around another duplex of the same molecule in an antiparallel configuration. Osmotic compression is important irrespective DNA topology. Accordingly, in order to understand compaction, these two aspects of the crowding phenomenon need to be evaluated and gauged against our observations.

An important feature of supercoiling is that it provides a mechanism to bring distant DNA sections, which are separated spatially, closer together. A schematic drawing of a branched supercoil is shown in Figure 5A. Note that a supercoil of the present molecular weight may be branched, but this is irrelevant for the present discussion. The two opposing duplexes are antiparallel and separated by a distance $r$ in the direction perpendicular to the central axis of the supercoil. Each duplex is surrounded by a cylindrical depletion zone of diameter $D + d$, with $D$ and $d$ being the diameter of the duplex and nanoparticle, respectively. As illustrated in Figure 5B, for interduplex distance $r$ in the range $D < r < D + d$ there is an attractive force due to the overlap of the depletion zones with concomitant increase in accessible volume to the nanoparticles. In crowded conditions, the supercoil is effectively confined within a cylindrical volume with a diameter equal to the sum of the diameter of the duplex and size of the crowder, that is, $D + d$. Note that a reduction in interduplex distance by increasing concentration of plasmid (DNA−DNA crowding) has previously been inferred from neutron scattering and Monte Carlo simulation.

The interwound supercoil can be considered a wormlike chain set out by the central (pletonic) axis with length $L_{plec}$ and bending persistence length $P_{plec}$. The persistence length is the projection of the persistence lengths of the two opposing duplexes (each with persistence length $P$) onto the central axis, that is, $P_{plec} = 2P \cos \theta$ with $\theta$ the angle enclosed by the duplex’s tangent vector and the central axis. The length of the central axis $L_{plec}$, angle $\theta$, and persistence length $P_{plec}$ can be obtained by minimization of the molecular free energy of the supercoil including elastic, electrostatic, and entropic contributions. With a similar theoretical approach, we obtained these structural parameters for a supercoil subjected to confinement within a cylindrical volume with diameter $D_{tube}$. Results are shown in panels C−E of Figure 5. With increasing confinement (smaller values of $D_{tube}$), both $L_{plec}$ and $P_{plec}$ are seen to increase due to increasing alignment (smaller values of $\theta$) of the segments. The supercoil expands due to this increase in length and bending rigidity of the superhelical axis.

With the contour and persistence length of the superhelical axis, $R_g$ of a nonbranched, wormlike supercoil can be calculated with the Benoit−Doty equation. Note that there are only a few Kuhn segments per supercoil [$L_{plec}/(2P_{plec}) \sim 2$], so that swelling due to self-avoidance is negligible. However, the absolute value of the calculated $R_g$ bears little relevance because the real supercoil is smaller in size than the hypothetical linear one due to branching. Accordingly, in Figure 5F the relative change in $R_g$ with respect to the unconfined situation is depicted. In crowded conditions, the supercoil is effectively confined within a tube with diameter $D_{tube} \approx D + d$. For confinement within a range corresponding to the size of the smallest nanoparticles, the predicted increase in $R_g$ is $\sim 14\%$. For the particles of intermediate size, the increase is $\sim 10\%$, whereas for the largest particles the effect is minimal with an increase of $\sim 2\%$. These theoretical predictions for the increase in $R_g$ are in almost quantitative agreement with the experimentally observed apex in $R_g$ for the plasmid in the

![Figure 5](image-url)
The critical volume fraction $R_{\text{g}}$ surrounding medium is to leading order given by $d_{\text{pol}}/kT \approx (R_0^2/R_g)^2$ with $R_0^2$ the radius of gyration in the absence of the compressing force. The elastic pressure follows from the derivative of the elastic free energy to the volume of the coil ($V \approx R_g^3$) and reads $\Pi_{\text{elas}} \approx kT R_g^{12}/R_g^3$. A scaling relation for the work of inserting a nanoparticle into the coil can be derived following a procedure originally due to de Gennes. The work is on the order of thermal energy and proportional to the ratio of the particle and coil size, that is, $w/kT \approx d/R_{\text{g}}^2$ (again, we assume ideal statistics). The coil is immersed in a medium with nanoparticle density $\rho$. From the balance in chemical potentials, the difference in particle density between the interior and surrounding medium is to leading order given by $\Delta \rho \approx \rho d/R_{\text{g}}$ ($d \ll R_{\text{g}}$). With a typical experimental ratio $d/R_{\text{g}} \approx 0.05$, the particle density is depleted by a few percent. The osmotic pressure $\Pi_{\text{osmo}} \approx kT \Delta \rho$ should balance the elastic pressure $\Pi_{\text{elas}} = \Pi_{\text{elas}}$ from which follows the scaling relation $R_{\text{g}} \approx R_0^2 \rho^{1/4} d^{-1/4}$.

In terms of the volume fraction of the nanoparticles ($f_{\phi} \approx \rho d^3$), this expression takes the form $R_{\text{g}} \approx R_0^{1/2} d^{1/4} f_{\phi}^{-1/4}$. At the onset of compaction $R_{\text{g}} \approx R_0$, which sets a critical volume fraction $f_{\phi} \approx (d/R_0^2)^{1/2}$. Accordingly, for linear DNAs the radius of gyration is already seen to decrease for intermediate size; see Figure 3A. However, the scaling theory does not correctly predict the strong dependence of $R_{\text{g}}$ on the size of the nanoparticles. This might be related to the above-described modification of the geometrical properties of the supercoil, which calls for a more detailed expression for the work of insertion. In view of the many uncertain parameters describing the intricate interaction between nanoparticles and supercoiled DNA, we refrain from further elaboration.

### CONCLUSIONS

With a view to understand compaction of DNA by crowding, we have measured the radius of gyration of a plasmid in its supercoiled and linear form and in the presence of neutral nanoparticles. The plasmid is sufficiently diluted, so that there is no significant DNA–DNA interaction. Our results show that in the context of supercoiling the crowding phenomenon has two aspects. First, the interduplex distance decreases, with a concomitant increase in length and bending rigidity of the superhelical axis. This is due to the depletion of nanoparticles in the overlap region between the two opposing duplexes of the superheli. Through this change in geometrical properties, the supercoil expands. The interduplex distance becomes around the range of the attractive force, that is, the sum of the radii of the duplex and nanoparticle. The decrease in interduplex distance with concomitant expansion of the supercoil is hence more conspicuous for crowders of smaller size. For larger nanoparticles, the range of attraction may exceed the diameter of the supercoil in the crowder-free state. In this situation, there is no effective confinement and hence no crowder-induced expansion of the supercoil. A second aspect of crowding is that the nanoparticle density in the interior of the coil is depleted, which results in an imbalance in osmotic pressure between the coil and the surrounding medium. The plasmid gets compacted, irrespective of topology, but does not collapse into a condensed state. The antagonistic nature of these two aspects of crowding has the effect that the size of supercoiled plasmid first increases, reaches an apex, and subsequently decreases with increased crowding. The maximum depends on the extent of the crowder-induced expansion, with the highest apex for the smallest crowders and vanishingly small or no apex for crowders of size equal to or larger than the interduplex distance in the crowder-free state. In the case of a linear plasmid, the only relevant mechanism is osmotic compression. Accordingly, the size of the linear plasmid decreases monotonously, and no apex is observed. A striking result is that in crowded conditions the size of supercoiled plasmid may exceed the one of its linear variant. In this situation, supercoiling restrains rather than facilitates compaction of DNA. Overall, macromolecular crowding in combination with supercoiling has a much more pronounced and richer effect on plasmid size than the effect of variation in ionic strength. This may have implications for the tuning of favorable configurational states of the genetic material in biology as well as biotechnology.

### ASSOCIATED CONTENT

#### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.macromol.6b02742.

Form factor expressions for linear and circular semiflexible polymers, agarose gel electrophoresis of closed circular and linear plasmid, and gel electrophoresis with chloroquine staining for linking number determination (PDF)

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### Notes

The authors declare no competing financial interest.

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### REFERENCES


(13) Fishman, D. M.; Patterson, G. D. Light scattering studies of supercoiled and nicked DNA. Biopolymers 1996, 38, 535–552.


(26) van der Maarel, J. R. C. Introduction to Biopolymer Physics; World Scientific: 2008.


